

# Resonance:

A resonator is something that can resonate, i.e., something that can vibrate or allows the propagation of waves. Examples:

- Ocean, lake (water waves)
- Vacuum (electromagnetic waves)
- air (sound waves)
- pipe, tube, flute, wind instrument
- string, metal bar, xylophone
- microwave or laser cavity
- RLC-circuit

Some resonators (ocean, interstellar space, air) allow waves of all wavelengths. Other resonators allow only waves with certain wavelengths. This phenomenon is called resonance.

An RLC circuit has a center frequency, where the attenuation of a vibration is minimal. This is called the resonance frequency. The width of the resonance is determined by the damping resistor.

Finite resonators may have boundary conditions (nodes or antinodes at the ends). There is a series of standing waves called harmonics which satisfy the boundary conditions. The harmonics are also called eigenmodes or eigenfrequencies, since the problem of solving the wave equation with boundary conditions is similar to finding the eigenvalues of matrix (linear algebra).

### **Strategy for solving resonant standing wave problems:**

What is the nature of the boundary conditions: Is there a node or an antinode on each end ?

Distance between two nodes:  $\lambda/2$

Distance between two antinodes:  $\lambda/2$

Distance between a node and an antinode:  $\lambda/4$

Standing waves on a string usually have nodes on both ends.

A standing sound wave has a node, if the end of the resonator (pipe) is closed. It has an antinode, if the end of the resonator is open.